

# Computer Vision Course

## Lecture 04

### Template Matching

### Image Pyramids

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Spring 2015

Last updated 11/03/2015

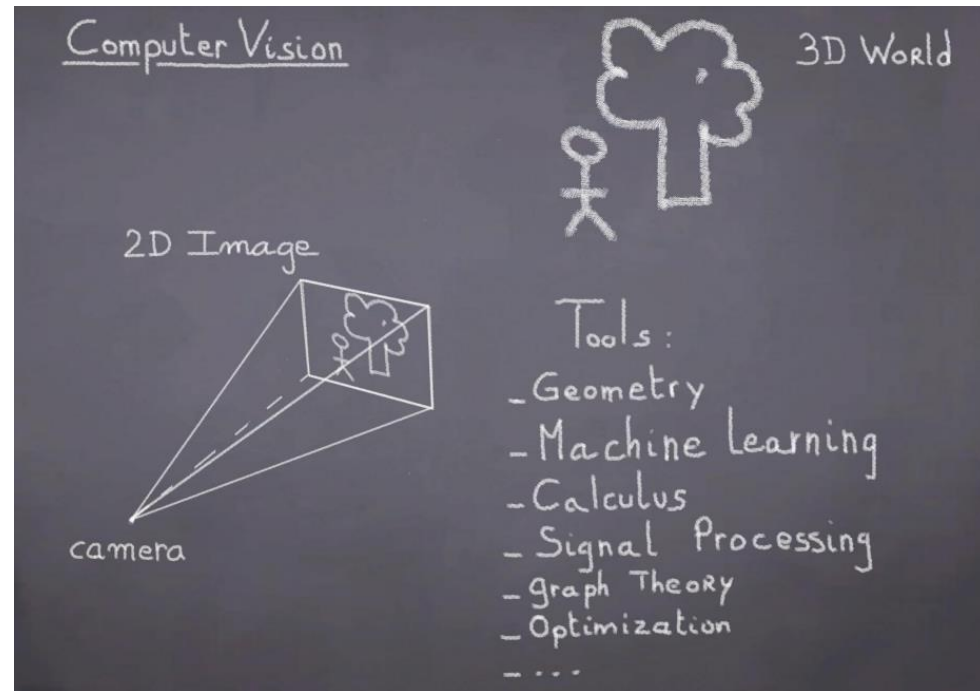


Photo credit: Olivier Teboul  
[vision.mas.ecp.fr/Personnel/teboul](http://vision.mas.ecp.fr/Personnel/teboul)

# Course Outline

## Image Formation and Processing

Light, Shape and Color

The Pin-hole Camera Model, The Digital Camera

Linear filtering, Template Matching, Image Pyramids

## Feature Detection and Matching

Edge Detection, Interest Points: Corners and Blobs

Local Image Descriptors

Feature Matching and Hough Transform

## Multiple Views and Motion

Geometric Transformations, Camera Calibration

Feature Tracking , Stereo Vision

## Segmentation and Grouping

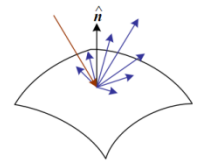
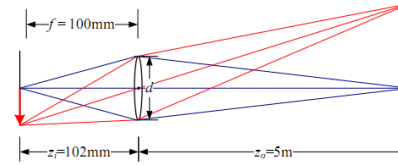
Segmentation by Clustering, Region Merging and Growing

Advanced Methods Overview: Active Contours, Level-Sets, Graph-Theoretic Methods

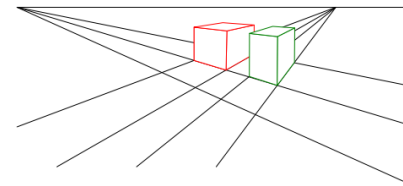
## Detection and Recognition

Problems and Architectures Overview


Statistical Classifiers, Bag-of-Words Model, Detection by Sliding Windows

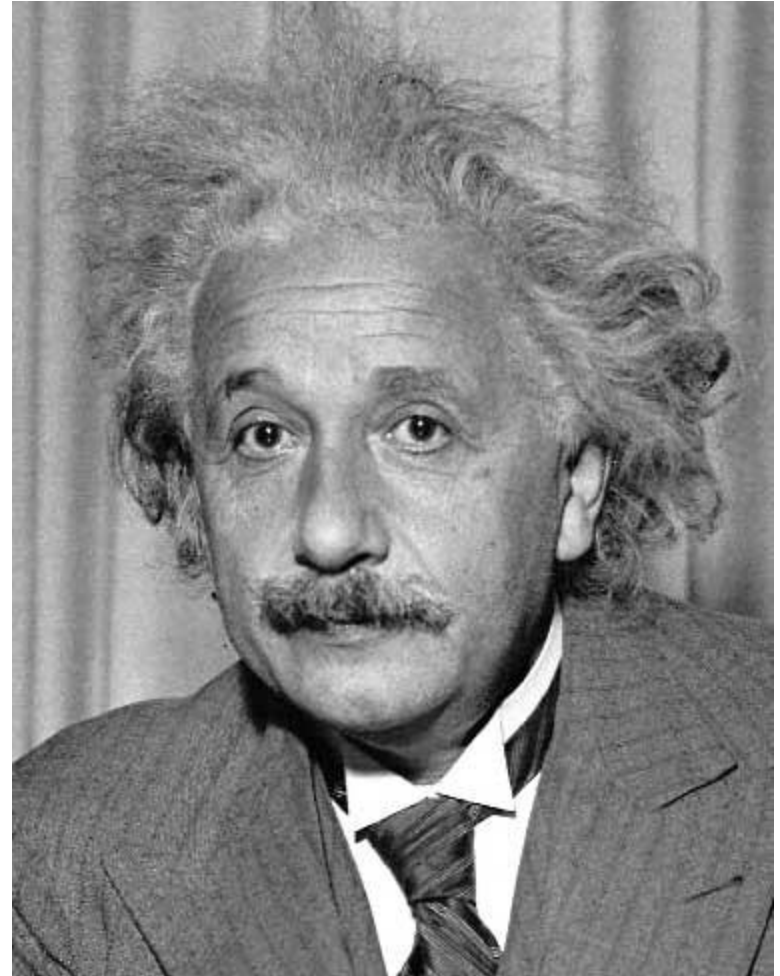


G	R	G	R
B	G	B	G
G	R	G	R
B	G	B	G



# Template Matching

- Goal: find  in image
- Main challenge: What is a good similarity or distance measure between two patches?
  - Correlation
  - Zero-mean correlation
  - Sum Square Difference
  - Normalized Cross Correlation

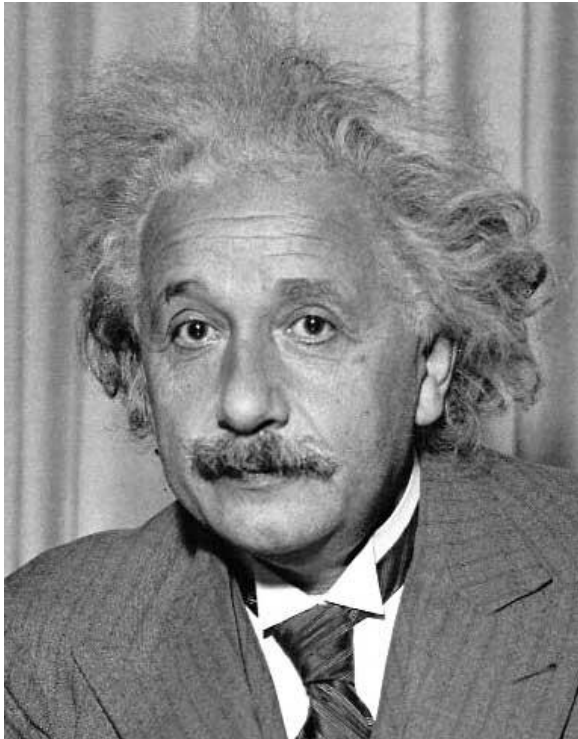


# Matching with Filters

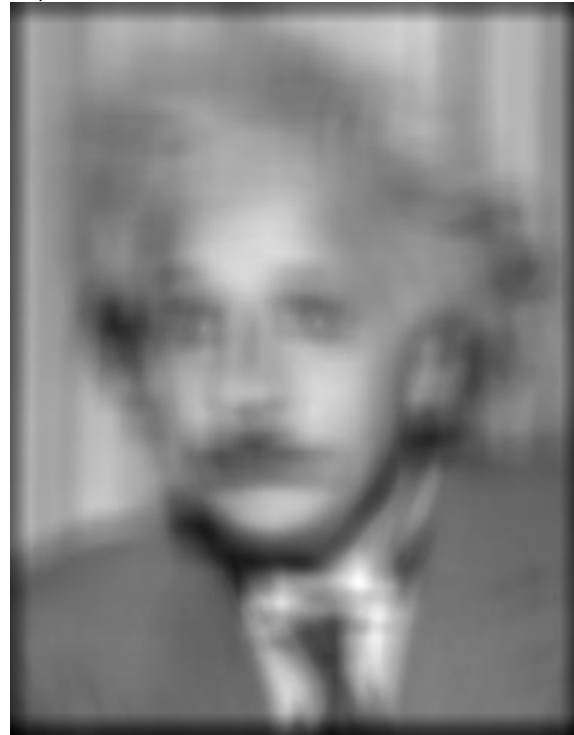
- Goal: find  in image
- Method 0: filter the image with eye patch

$$h[m,n] = \sum_{k,l} g[k,l] f[m+k,n+l]$$

f = image  
g = filter



Input



Filtered Image

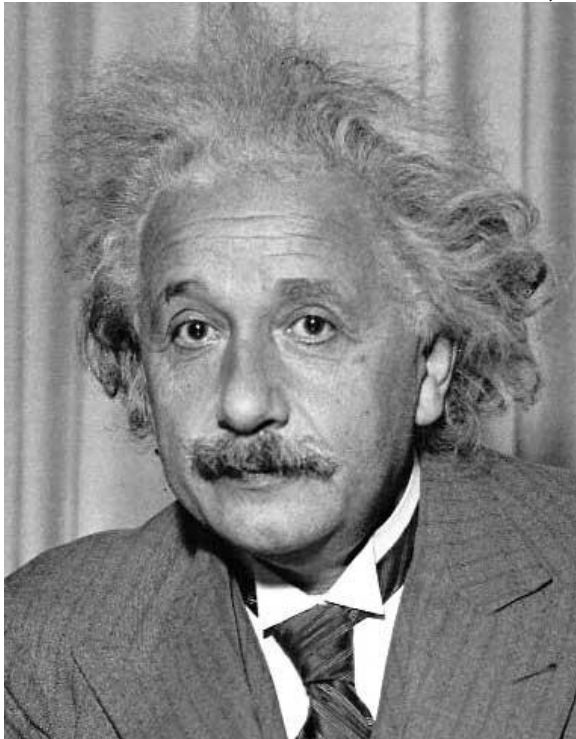
What went wrong?

# Matching with Filters

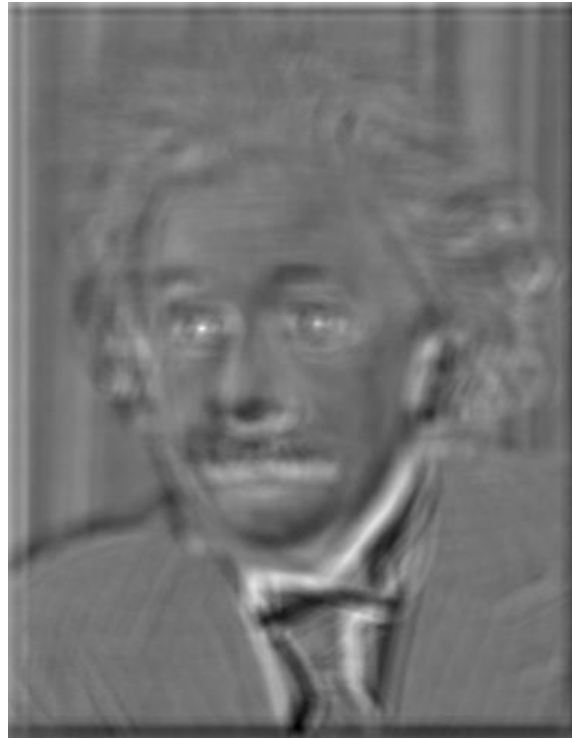
- Goal: find  in image
- Method 1: filter the image with zero-mean eye

$$h[m,n] = \sum_{k,l} (f[k,l] - \bar{f})(g[m+k, n+l])$$

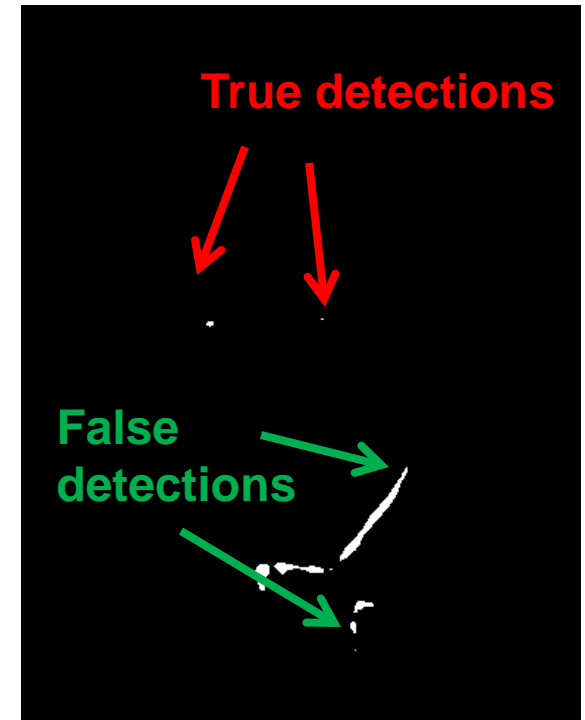
$\bar{f}$  ← mean of  $f$



Input



Filtered Image (scaled)

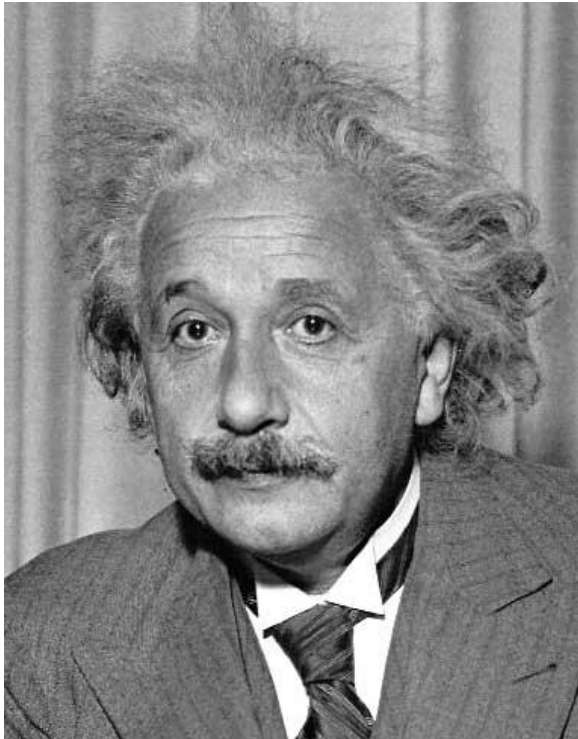


Thresholded Image

# Matching with Filters

- Goal: find  in image
- Method 2: SSD

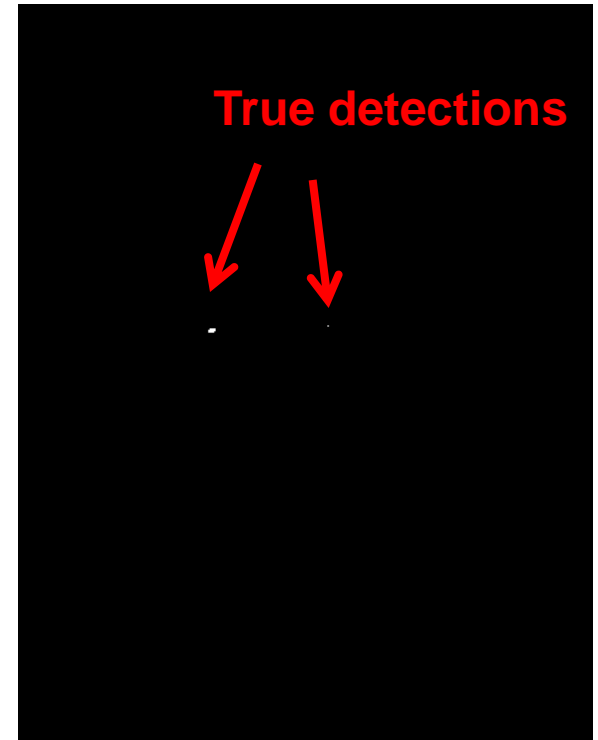
$$h[m,n] = \sum_{k,l} (g[k,l] - f[m+k,n+l])^2$$



Input



1- sqrt(SSD)



Thresholded Image

# Matching with Filters

Can SSD be implemented with linear filters?

$$h[m,n] = \sum_{k,l} (g[k,l] - f[m+k,n+l])^2$$

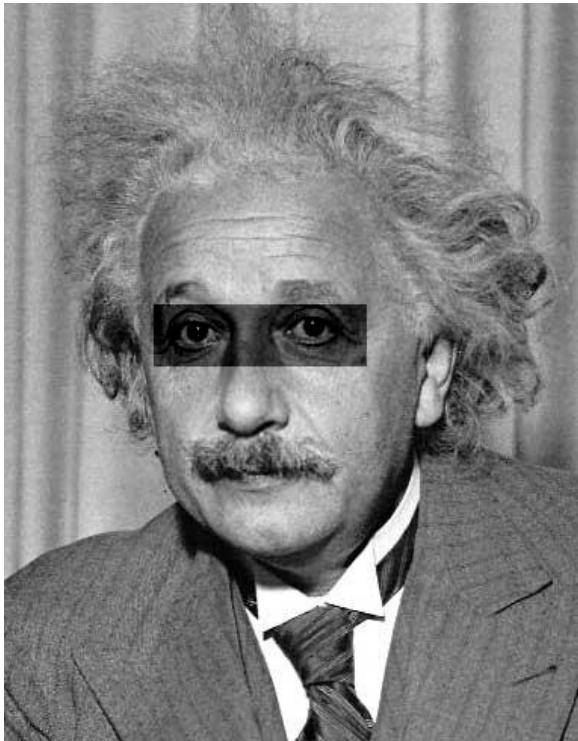


# Matching with Filters

- Goal: find  in image
- Method 2: SSD

What's the potential  
downside of SSD?

$$h[m,n] = \sum_{k,l} (g[k,l] - f[m+k,n+l])^2$$



Input



1- sqrt(SSD)



# Matching with Filters

- Goal: find  in image
- Method 3: Normalized cross-correlation


$$h[m,n] = \frac{\sum_{k,l} (g[k,l] - \bar{g})(f[m-k,n-l] - \bar{f}_{m,n})}{\left( \sum_{k,l} (g[k,l] - \bar{g})^2 \sum_{k,l} (f[m-k,n-l] - \bar{f}_{m,n})^2 \right)^{0.5}}$$

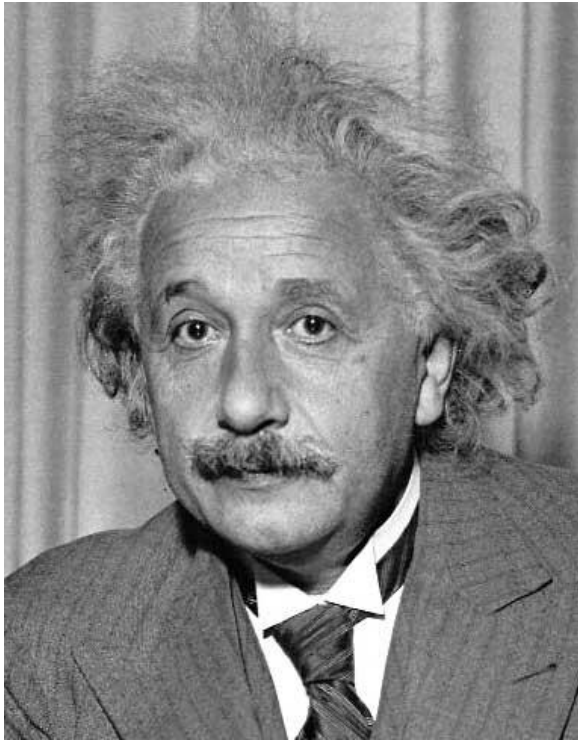
mean template                      mean image patch

↓    ↓

Matlab: `normxcorr2(template, im)`

# Matching with Filters

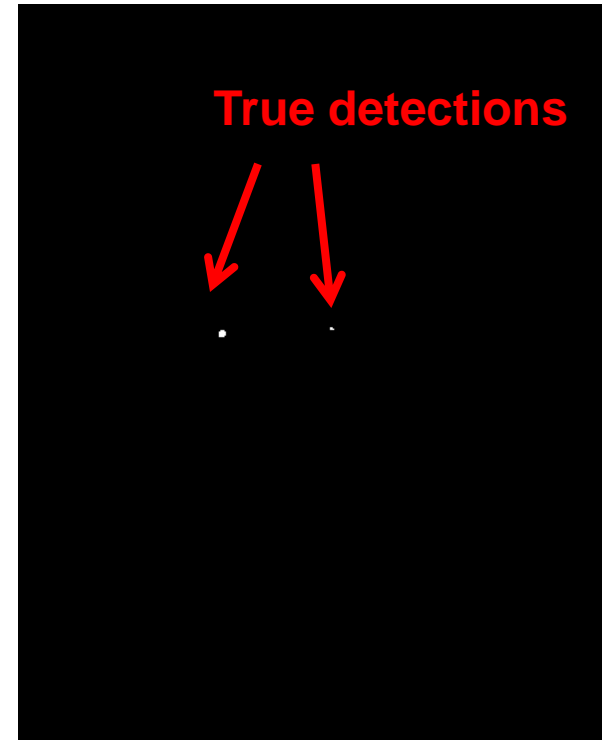
- Goal: find  in image
- Method 3: Normalized cross-correlation



Input




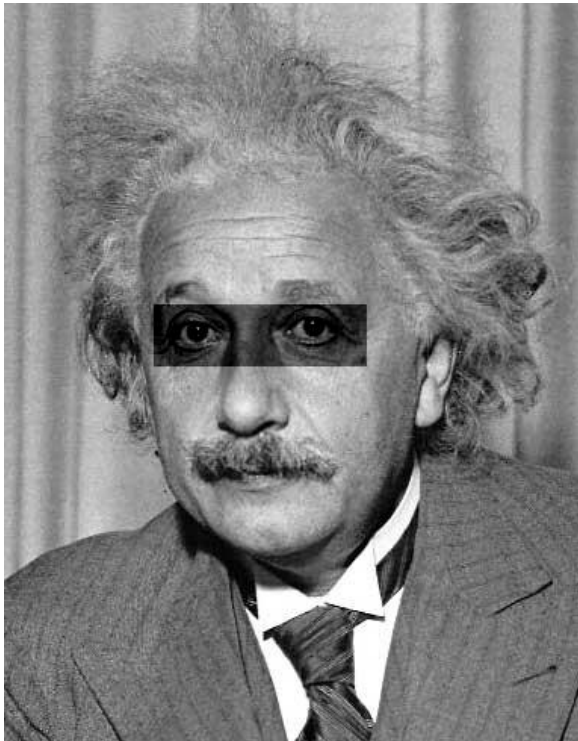
Normalized X-Correlation



Thresholded Image

# Matching with Filters

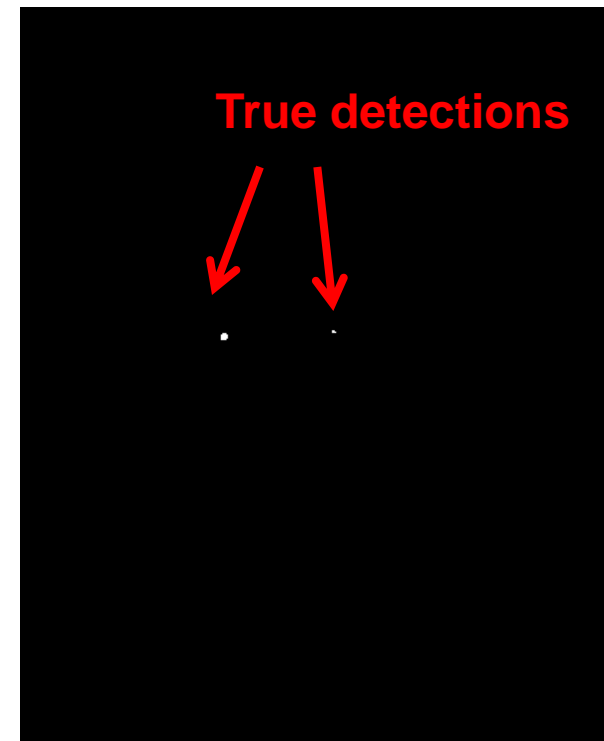
- Goal: find  in image
- Method 3: Normalized cross-correlation



Input



Normalized X-Correlation



Thresholded Image

# Q: What is the best method to use?

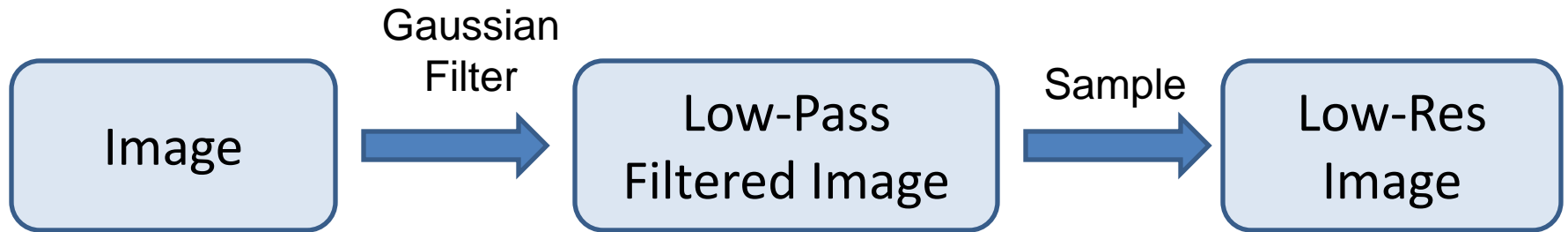
A: Depends

- SSD: faster, sensitive to overall intensity
- Normalized cross-correlation: slower, invariant to local average intensity and contrast
- But really, neither of these baselines are representative of modern recognition.

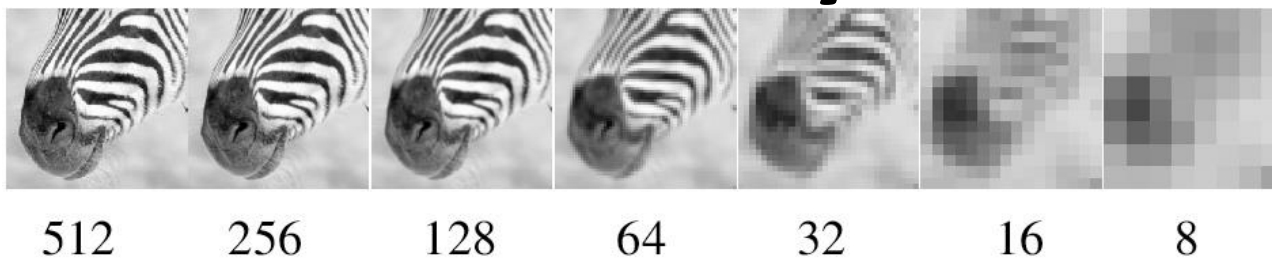
**Q: What if we want to find larger or smaller eyes?**

A: Image Pyramid

# Review of Sampling



# Gaussian Pyramid





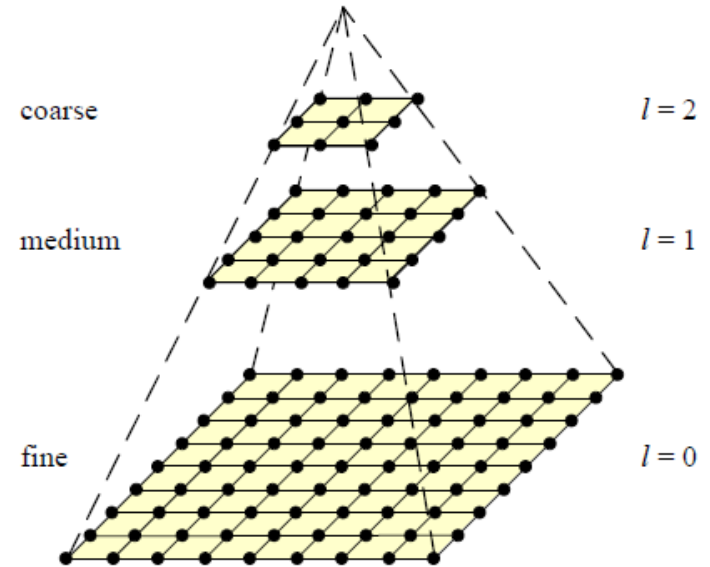
# Template Matching with Image Pyramids

Input: Image, Template

1. Match template at current scale
2. Downsample image
3. Repeat 1-2 until image is very small
4. Take responses above some threshold, perhaps with non-maxima suppression

# Coarse-to-Fine Image Registration

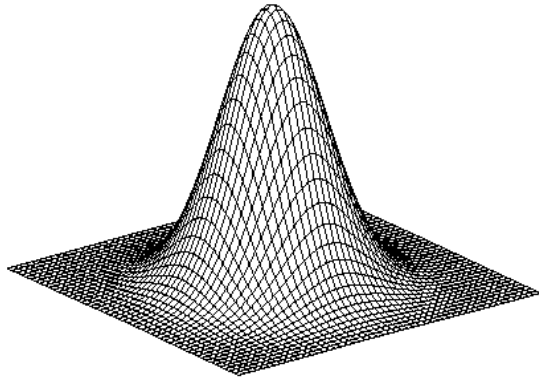
1. Compute Gaussian pyramid
2. Align with coarse pyramid
3. Successively align with finer pyramids
  - Search smaller range



Why is this faster?

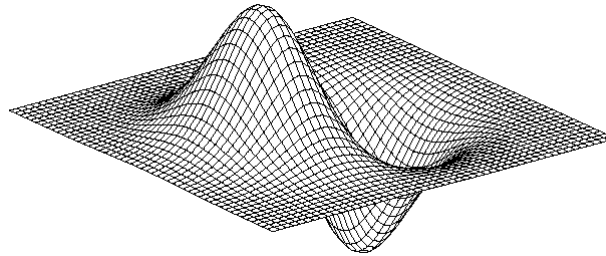
Are we guaranteed to get the same result?

# 2D Edge Detection Filters



Gaussian

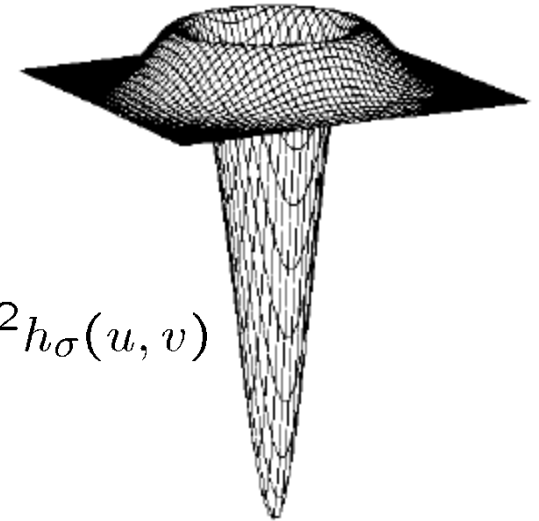
$$h_{\sigma}(u, v) = \frac{1}{2\pi\sigma^2} e^{-\frac{u^2+v^2}{2\sigma^2}}$$



derivative of Gaussian

$$\frac{\partial}{\partial x} h_{\sigma}(u, v)$$

Laplacian of Gaussian

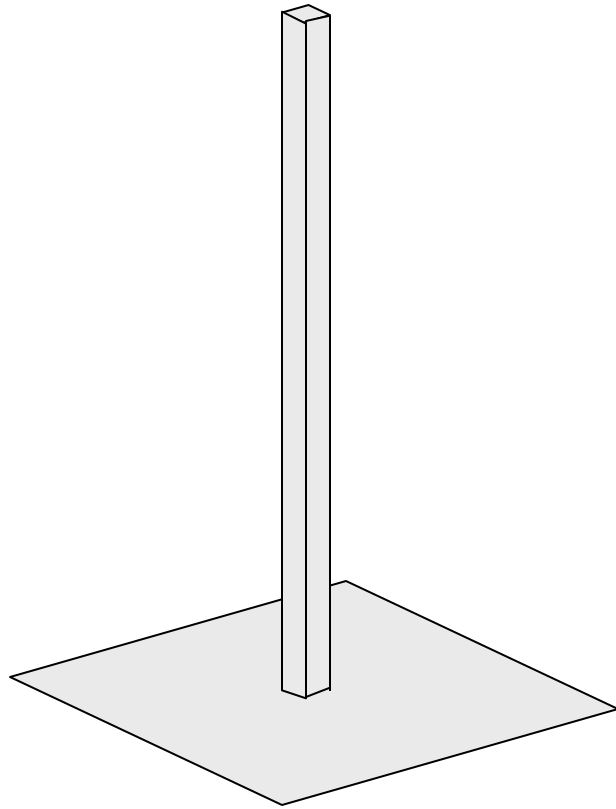


$$\nabla^2 h_{\sigma}(u, v)$$

$\nabla^2$  is the **Laplacian** operator:

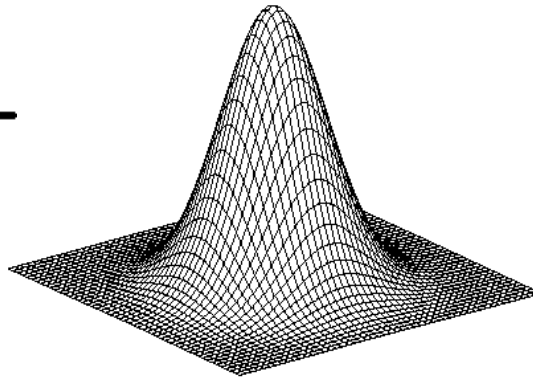
$$\nabla^2 f = \frac{\partial^2 f}{\partial x^2} + \frac{\partial^2 f}{\partial y^2}$$

# Laplacian Filter



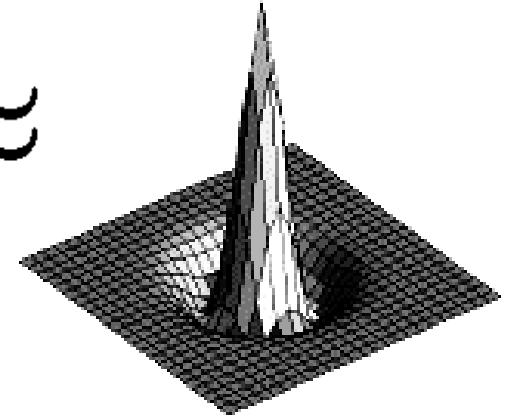
unit impulse

—



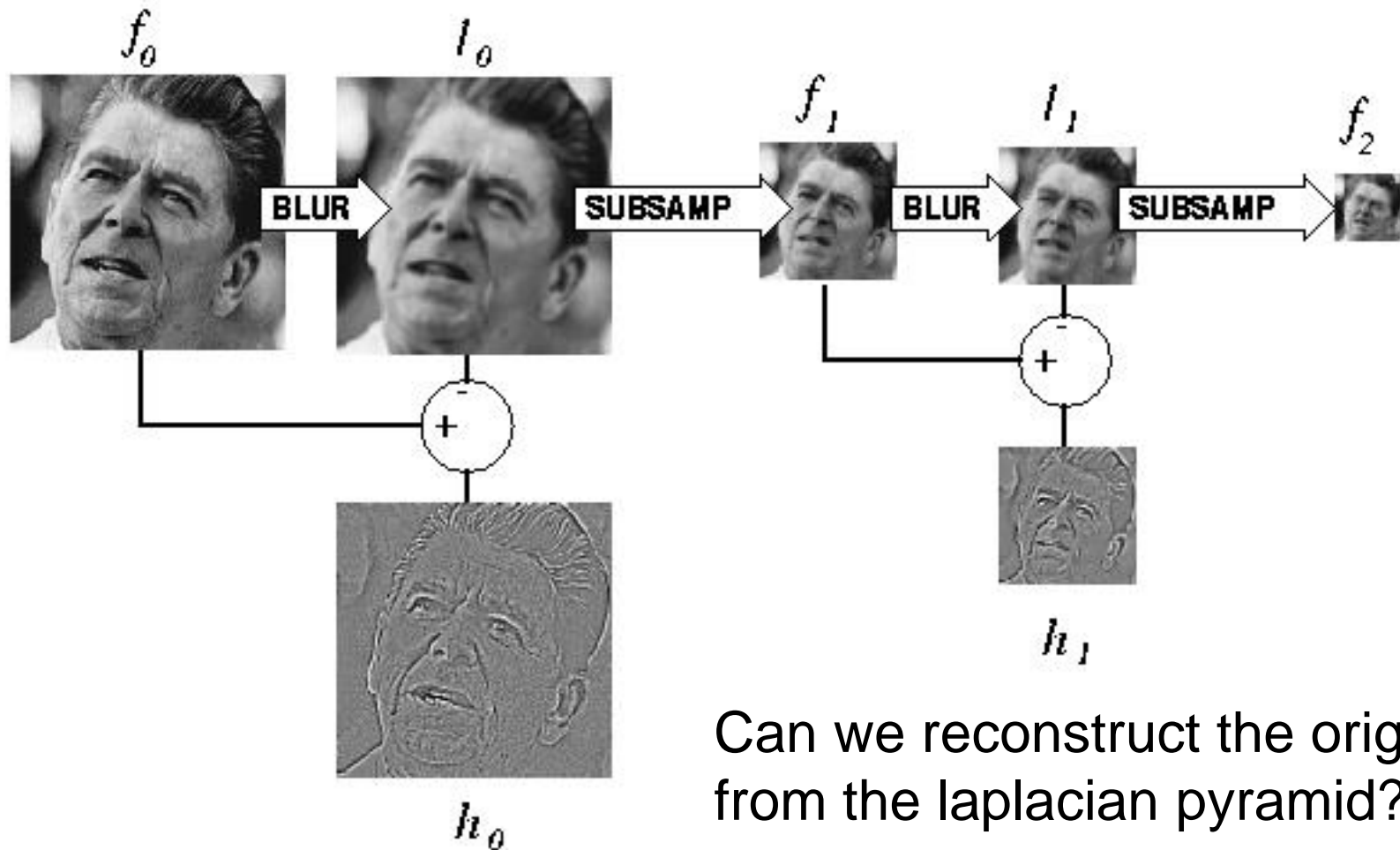
Gaussian

$\approx$



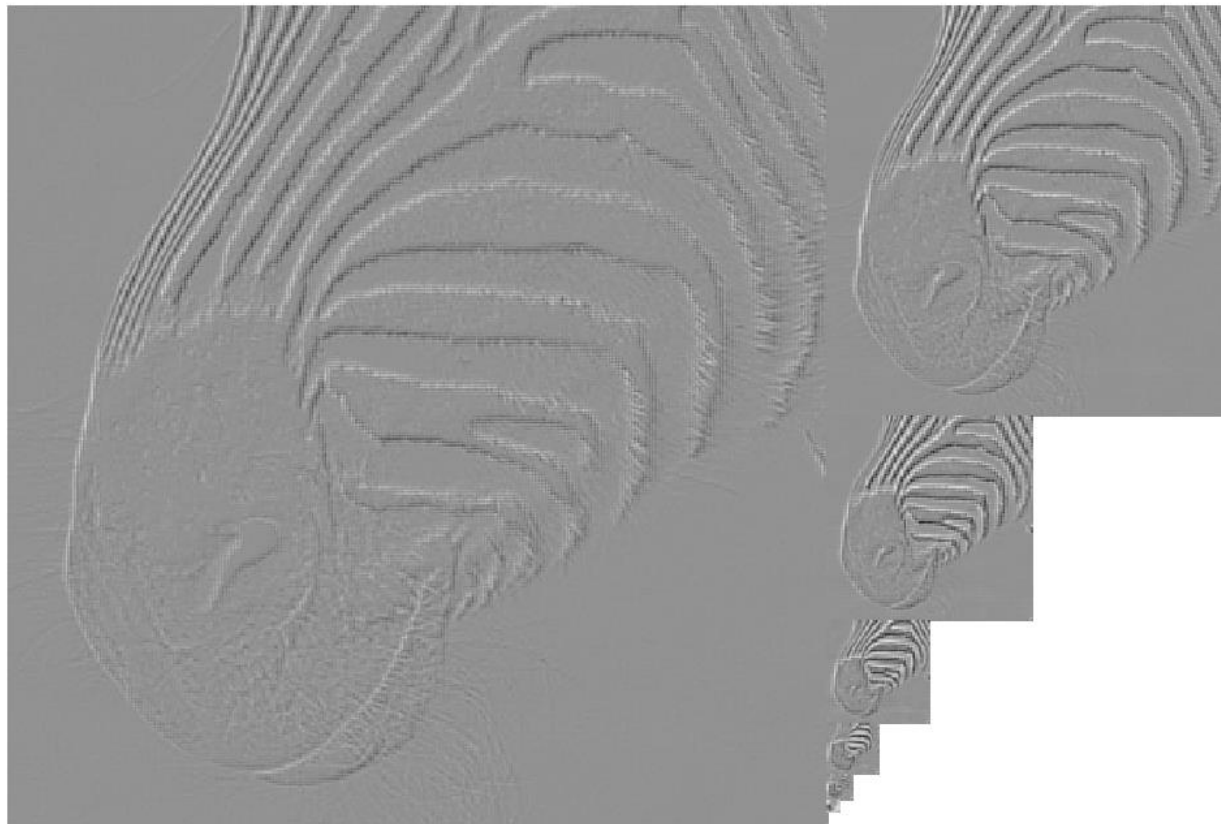
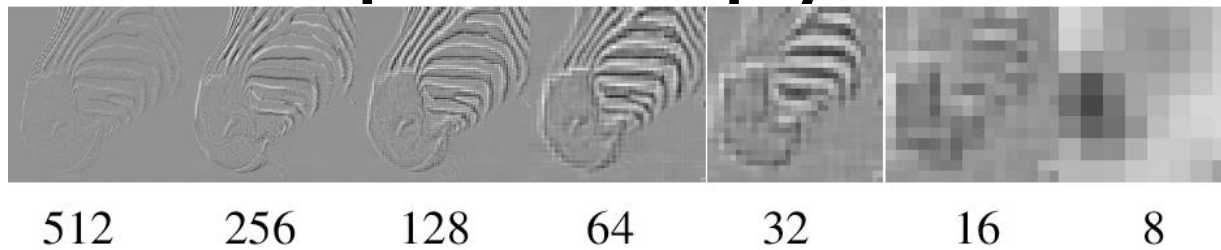
Laplacian of Gaussian

# Computing Gaussian/Laplacian Pyramid



Can we reconstruct the original from the laplacian pyramid?

# Laplacian pyramid



# Major uses of image pyramids

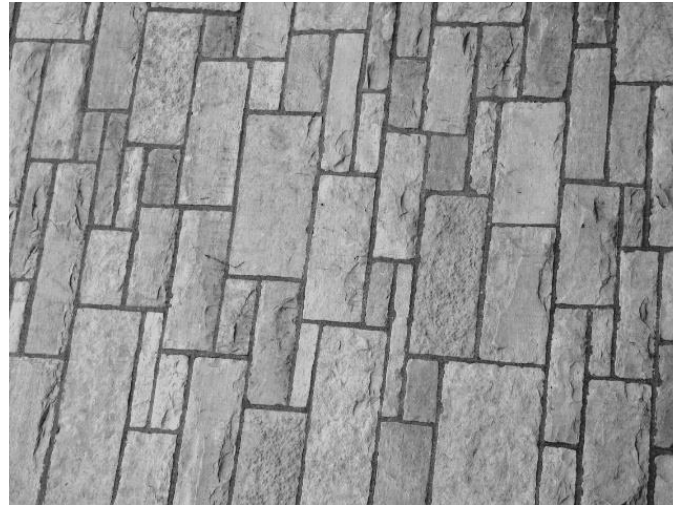
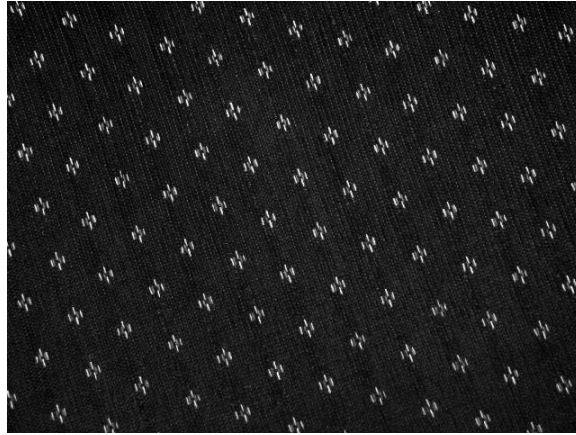
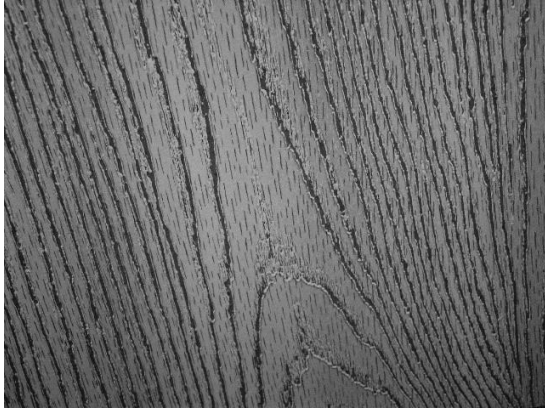
- Compression
- Object detection
  - Scale search
  - Features
- Detecting stable interest points
- Registration
  - Course-to-fine



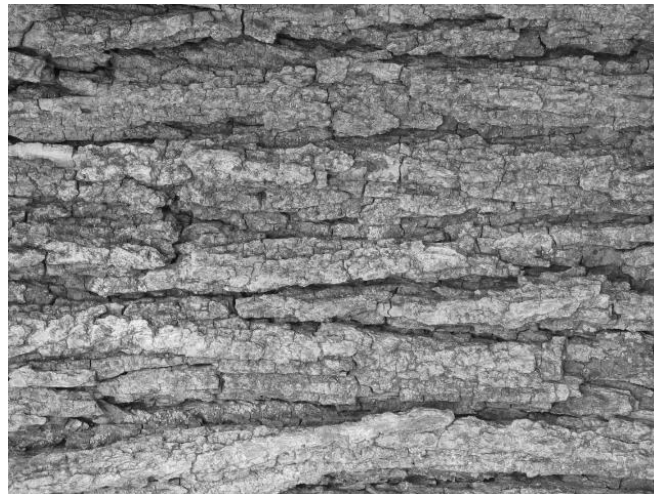
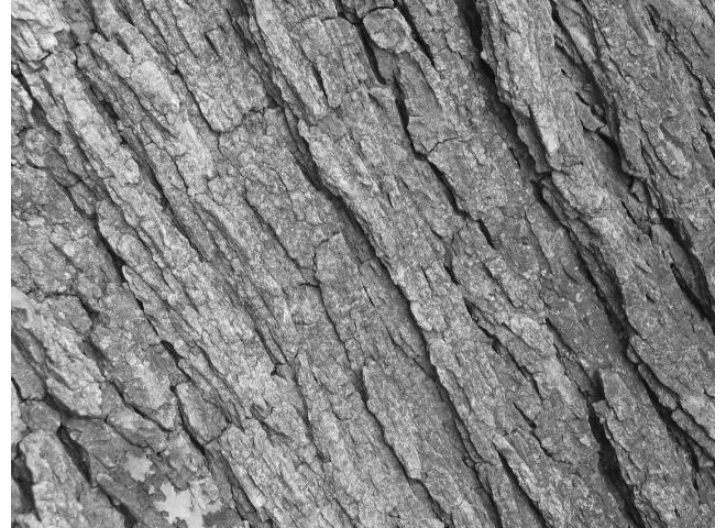
# Application: Representing Texture



# Texture and Material



# Texture and Orientation



# Texture and Scale



# What is texture?

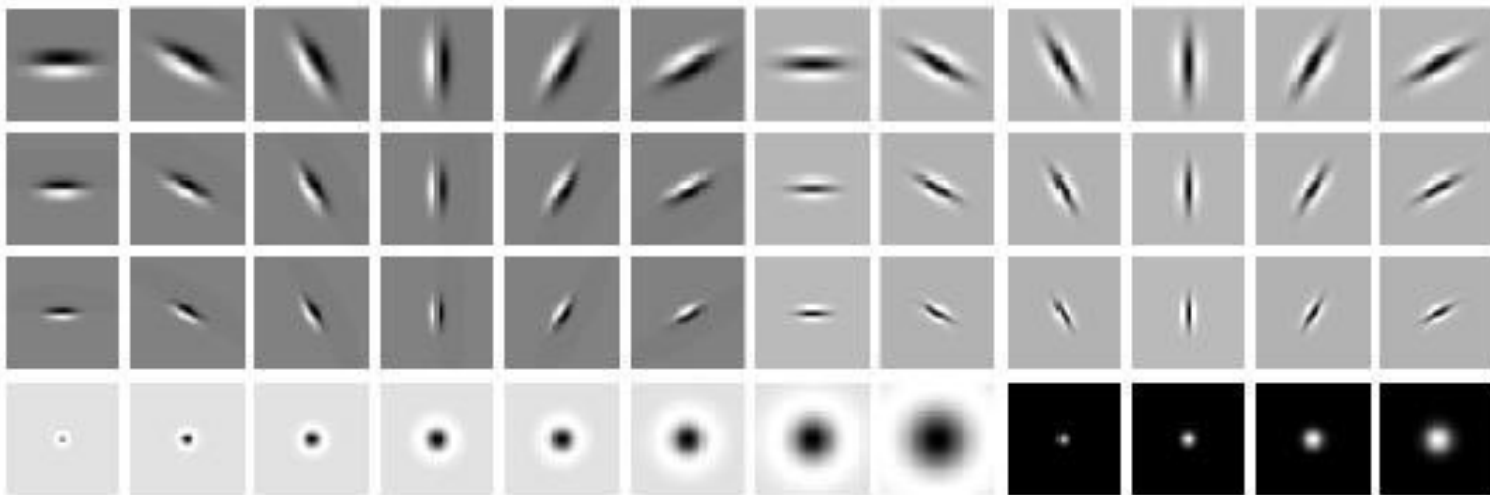
Regular or stochastic patterns caused by bumps, grooves, and/or markings

# How can we represent texture?

- Compute responses of blobs and edges at various orientations and scales

# Overcomplete representation: filter banks

LM Filter Bank

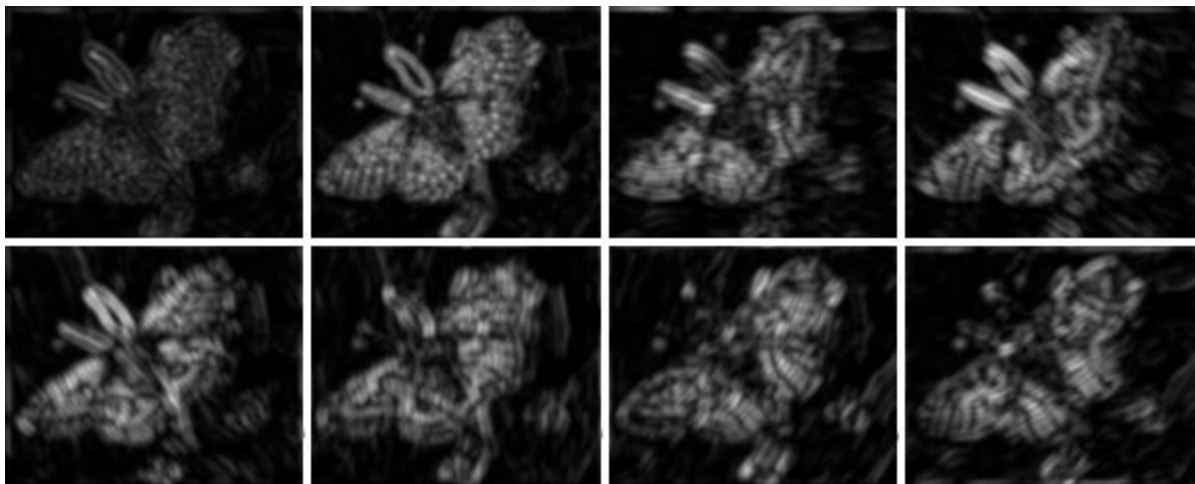
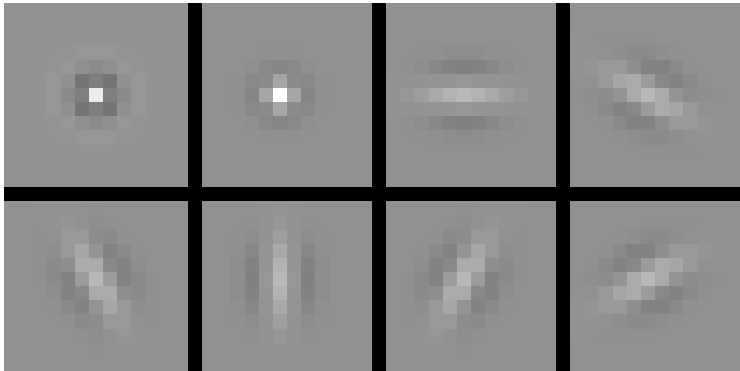


Code for filter banks: [www.robots.ox.ac.uk/~vgg/research/texclass/filters.html](http://www.robots.ox.ac.uk/~vgg/research/texclass/filters.html)



# Filter banks

- Process image with each filter and keep responses (or squared/abs responses)

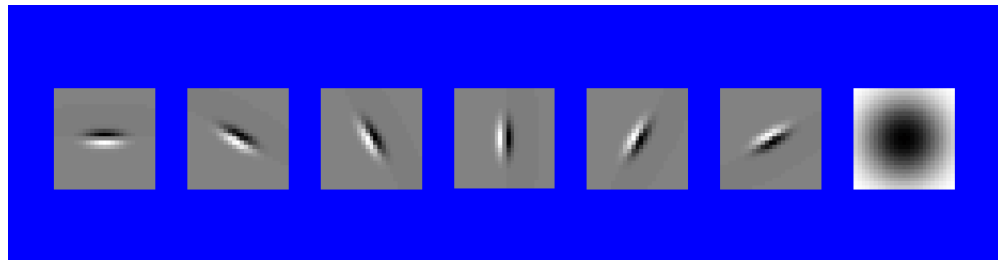


# How can we represent texture?

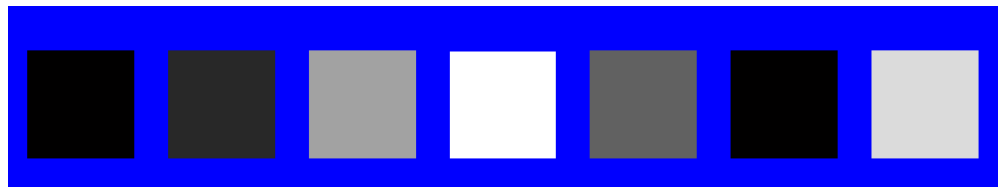
- Measure responses of blobs and edges at various orientations and scales
- Idea 1: Record simple statistics (e.g., mean, std.) of absolute filter responses

# Can you match the texture to the response?

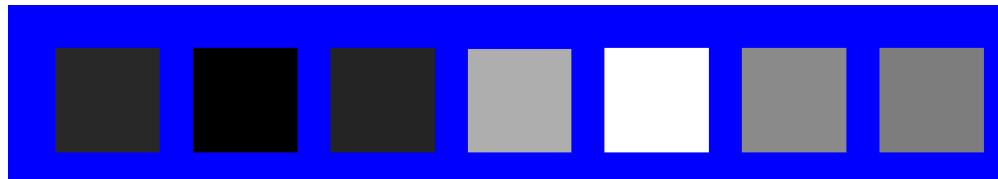
Filters



1



2

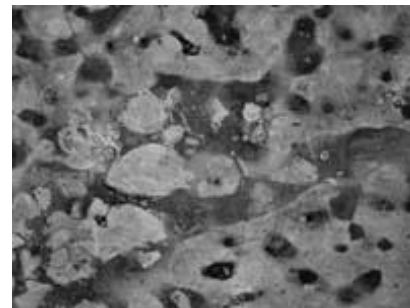


3



Mean abs responses

A



B

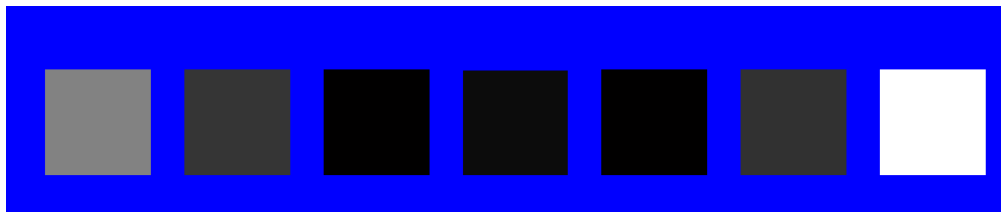
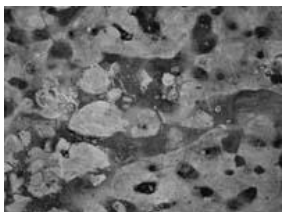
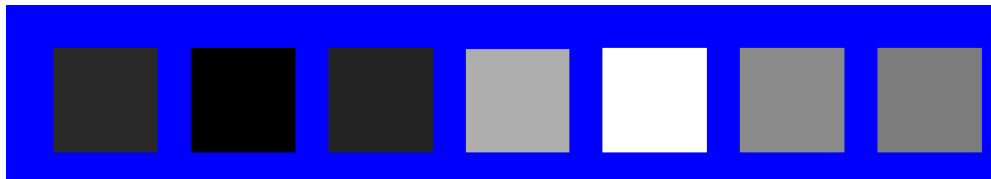
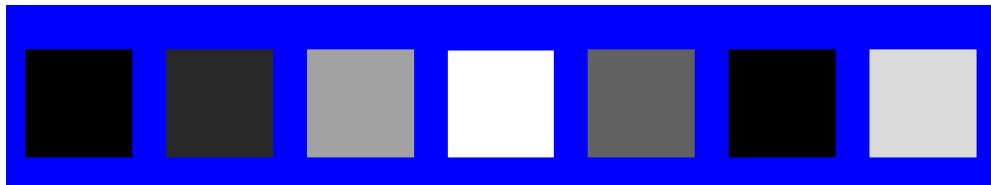
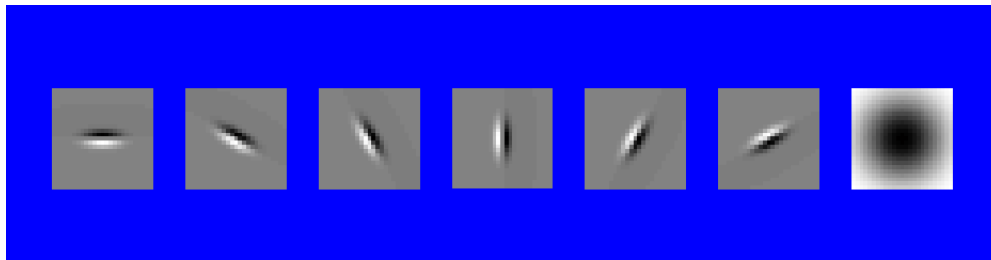


C



# Representing texture by mean abs response

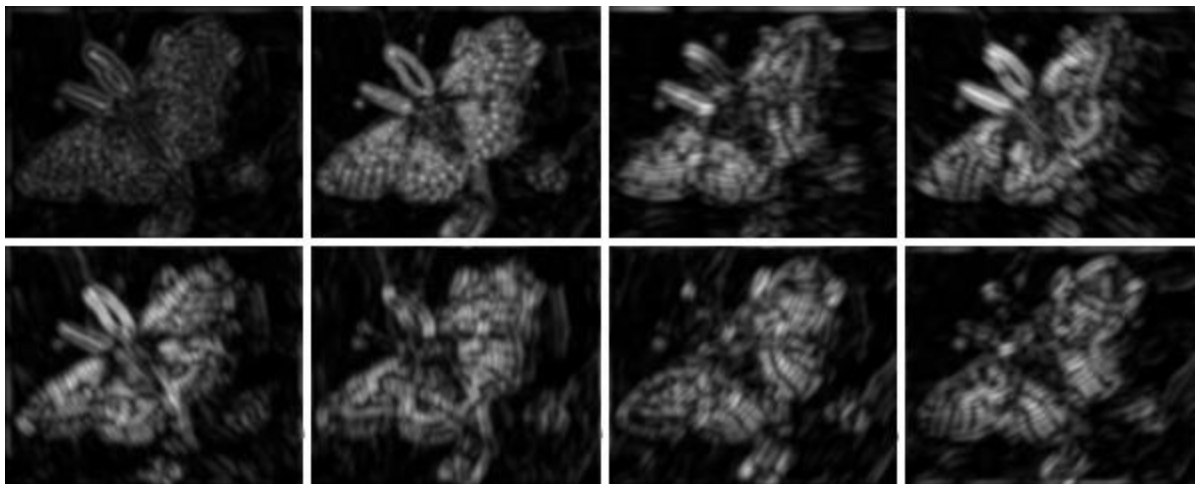
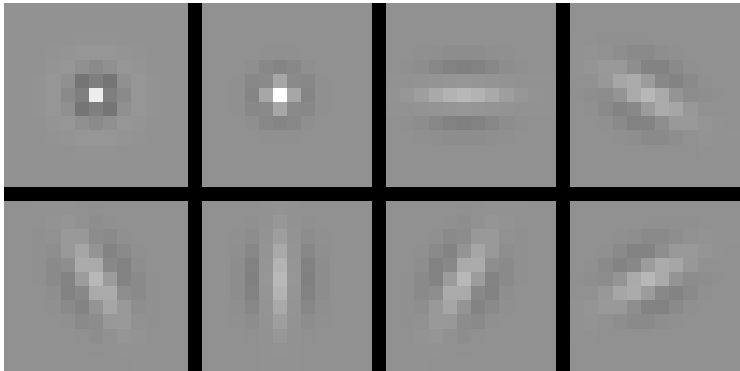
Filters



Mean abs responses

# Representing texture

- Idea 2: take vectors of filter responses at each pixel and cluster them, then take histograms (more on in later weeks)



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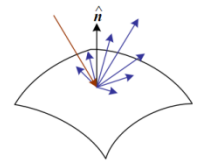
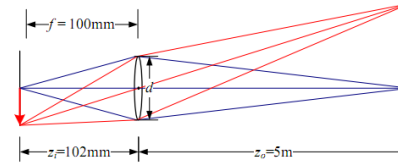
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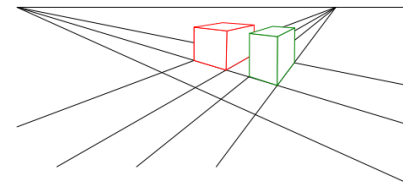
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G	R	G	R
B	G	B	G
G	R	G	R
B	G	B	G



# Resources

## Books

R. Szeliski, Computer Vision: Algorithms and Applications, 2010 – *available online*

D. A. Forsyth and J. Ponce, Computer Vision: A Modern Approach, 2003

L. G. Shapiro and G. C. Stockman, Computer Vision, 2001

## Web

**CVonline: The Evolving, Distributed, Non-Proprietary, On-Line Compendium of Computer Vision**

<http://homepages.inf.ed.ac.uk/rbf/CVonline/>

**Dictionary of Computer Vision and Image Processing**

<http://homepages.inf.ed.ac.uk/rbf/CVDICT/>

**Computer Vision Online**

<http://www.computervisiononline.com/>

## Programming

**Development environments/languages:** Matlab, Python and C/C++

**Toolboxes and APIs:** OpenCV, VLFeat Matlab Toolbox, Piotr's Computer Vision Matlab Toolbox, EasyCamCalib Software, FLANN, Point Cloud Library PCL, LibSVM, Camera Calibration Toolbox for Matlab